

MODELING AND IDENTIFICATION OF BALL SCREW FEED DRIVE SYSTEMS

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Abstract— In this paper, the ball screw feed drive system is simulated and it's frequency response is studied. Various parameters effect on the dynamic behavior of the ball screw system have been investigated. Ball screw feed drive system is used in high speed machine tools due to their high efficiency. Estimation of the dynamic behavior of ball screw feed drive mechanism is very important in the industrial processes in order to get high demand for precision and accuracy in machine tools. Optimizing the drive operation can provide significant cost savings. A four degree of freedom system, lumped parameter model is used for modeling a single axis ball screw feed drive system and use it to study and analyze vibrations in this model. The mathematical modeling provides an important information about frequency response when applying different levels of table mass, stiffness of the nut, axial stiffness of the ball screw shaft and torsional stiffness of the ball screw on the system, to describe the effects of these parameters on the system dynamic behavior. The study of dynamic response of ball screw feed drive system provides a better performance control and better understanding of ball screw dynamics.

Keywords- Ball screw, Feed drive, Machine tool, Modeling, Vibrations

I. NOMENCLATURE

- J_m = inertia moment of the motor (kg.m2)
- J_s = inertia moment of the ball screw (kg.m2)
- M_s = the mass of ball screw (kg)
- M_t = the mass of working table (kg)
- Q_m = rotational viscous damping coefficient of the motor (N.s/m)
- Q_b = rotational viscous damping coefficient of the support bearing of ball screw (N.s/m)
- C_b = viscous damping coefficient of the supporting bearing of the ball screw (N.s/m)
- C_t = viscous damping coefficient of the guide way of the working table (N.s/m)

 $K_n = stiffness of the nut (N/m)$

- K_t = torsional stiffness of the ball screw shaft (N.m/rad)
- K_a = equivalent axial stiffness of ball screw shaft (N/m)
- R = angle conversion axial displacement of the constant
- "angle conversion from rotational to axial displacement" T = motor torque (N.m)
- X_s = axial displacement of the ball screw shaft (m)
- X_t = axial displacement of the working table (m)
- $\theta_{\rm m}$ = rotation angle of the motor (rad)
- θ_s = rotation angle of the ball screw shaft (rad)

II. INTRODUCTION

The quality and productivity of machine tools production depend on their performance; the speed and positioning accuracy of feed drive system. The main purpose of its function is to move the cutting tool and work piece to the desired location and positioning the working parts of machine tools [1]. Comparing to other traditional linear actuators, Ball screw feed drive system is widely used in advanced industrial machinery due to their high efficiency and high positioning accuracy. It translates the rotational motion of a motor drive into a linear motion. Vibrations of ball screw feed drive system exist because of friction and interaction force between the balls, screw and nut. The values of these forces change with different position of the orbital system [2]. Most of the previous researches are concerned with reducing the existing vibrations and studying the variables that affect them. Many parameters such as table mass, stiffness of the ball nut, axial stiffness of the ball screw shaft and torsional stiffness of the ball screw have high effect on the frequency response of the system. So using mathematical model provide a better way to study these parameters [3, 4 and 5].

The vibration of ball screw feed drive system may be characterized by more than one mode of motion. It can be characterized by lateral, axial and torsional [6 and 7]. In this paper concerned with the hybrid modeling of a single axis ball screw feed drive system and consider the system consists of four degrees of freedom [4 and 7]. The mathematical model



estimates the quantitative dynamic behavior of the ball screw feed drive system. By substituting the measured parameters of the system on the mathematical model, we can study the effect of each parameter on the frequency response of ball screw feed drive system.

III. MATHEMATICAL MODELLING

A. Modeling of Feed Drive System –

In general, ball screw feed drive system consists of motor, coupler, screw shaft, ball screw nut, balls, support bearing and work table. This investigation interested with studying the modeling and vibration of a single axis ball screw feed drive system as shown in Fig. (1).



Fig. (1): A single axis ball screw feed drive system.

In this system, the authors try to make a model of the ball screw feed drive system by transforming the physical representation of it to equations and using these equations to simulate the system. A single axis ball screw feed drive system can be represented by a four displacements which consist of both axial and rotational displacements, Fig. (2) shows the schematic diagram of a ball screw feed drive system [3].



Fig. (2): Schematic diagram of a ball screw feed drive system.

The equations of a general multi-degree-of-freedom system are derived using the potential and kinetic energies and use them in deriving the equations of motion.

The kinetic energy of the system, T, can be expressed as

$$T = \frac{1}{2}J_m \theta_m^{.2} + \frac{1}{2}J_s \theta_s^{.2} + \frac{1}{2}M_s X_s^{.2} + \frac{1}{2}M_t X_t^{.2}$$

The mass matrix can be expressed as

$$[M_{model}] = \begin{bmatrix} J_m & 0 & 0 & 0 \\ 0 & J_s & 0 & 0 \\ 0 & 0 & M_s & 0 \\ 0 & 0 & 0 & M_t \end{bmatrix}$$

The dissipated energy of the system which refer to the energy that is lost from the system"D", can be expressed as

$$D = \frac{1}{2}Q_m\theta_m^{2} + \frac{1}{2}Q_b\theta_s^{2} + \frac{1}{2}C_bX_s^{2} + \frac{1}{2}C_tX_t^{2}$$

The damping matrix can be expressed as

$$\begin{bmatrix} C_{model} \end{bmatrix} = \begin{bmatrix} Q_m & 0 & 0 & 0 \\ 0 & Q_b & 0 & 0 \\ 0 & 0 & C_b & 0 \\ 0 & 0 & 0 & C_t \end{bmatrix}$$

The potential energy of the system, V, due to the strain energy of the springs, can be expressed as

$$\begin{split} V &= \frac{1}{2} K_t (\theta_m - \theta_s)^2 + \frac{1}{2} K_a X_s^2 + \frac{1}{2} K_n (R\theta_s + X_s - X_t)^2 \\ V &= \frac{1}{2} K_t \theta_m^2 + \frac{1}{2} K_t \theta_s^2 - \frac{1}{2} \times 2 K_t \theta_m \theta_s \\ &+ \frac{1}{2} K_a X_s^2 + \frac{1}{2} K_n (R^2 \theta_s^2 \\ &+ R\theta_s X_s - R\theta_s X_t + R\theta_s X_s + X_s^2 \\ &- X_s X_t - R\theta_s X_t - X_s X_t + X_t^2) \\ V &= \frac{1}{2} K_t \theta_m^2 + \frac{1}{2} K_t \theta_s^2 - \frac{1}{2} \times 2 K_t \theta_m \theta_s \\ &+ \frac{1}{2} K_a X_s^2 + \frac{1}{2} K_n R^2 \theta_s^2 + \frac{1}{2} K_n R \theta_s X_s \end{split}$$

$$-\frac{1}{2}K_{n}R\theta_{s}X_{t} + \frac{1}{2}K_{n}R\theta_{s}X_{s} + \frac{1}{2}K_{n}X_{s}^{2}$$

$$-\frac{1}{2}K_{n}X_{s}X_{t} - \frac{1}{2}K_{n}R\theta_{s}X_{t} - \frac{1}{2}K_{n}X_{s}X_{t} + \frac{1}{2}K_{n}X_{t}^{2}$$

$$V = \frac{1}{2}K_{t}\theta_{m}^{2} + \frac{1}{2}(K_{t} + K_{n}R^{2})\theta_{s}^{2} - \frac{1}{2} \times 2K_{t}\theta_{m}\theta_{s}$$

$$+ \frac{1}{2}(K_{a} + K_{n})X_{s}^{2} + \frac{1}{2}(K_{n}R + K_{n}R)\theta_{s}X_{s}$$

$$-\frac{1}{2}(K_{n}R + K_{n}R)\theta_{s}X_{t} - \frac{1}{2}(K_{n} + K_{n})X_{s}X_{t} + \frac{1}{2}K_{n}X_{t}^{2}$$

$$V = \frac{1}{2}K_{t}\theta_{m}^{2} + \frac{1}{2}(K_{t} + K_{n}R^{2})\theta_{s}^{2}$$

$$-\frac{1}{2} \times 2K_{t}\theta_{m}\theta_{s} + \frac{1}{2}(K_{a} + K_{n})X_{s}^{2}$$

$$+ \frac{1}{2} \times 2K_{n}R\theta_{s}X_{s} - \frac{1}{2} \times 2K_{n}R\theta_{s}X_{t}$$

$$-\frac{1}{2} \times 2K_{n}R\theta_{s}X_{s} + \frac{1}{2}K_{n}X_{t}^{2}$$

The stiffness matrix can be expressed as

$$[K_{model}] = \begin{bmatrix} K_t & -K_t & 0 & 0\\ -K_t & K_t + K_n R^2 & K_n R & -K_n R\\ 0 & K_n R & K_a + K_n & -K_n\\ 0 & -K_n R & -K_n & K_n \end{bmatrix}$$

The general form of the equations of motion is formulated in matrix form as:

[J _n 0 0 0	I_{i} J_{i} I_{i} I_{i}) 0 5 0 9 <i>M</i> 9 0) () (s () M	$\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ t_t \end{bmatrix} \times$	$\begin{cases} \theta_{m}^{-} \\ \theta_{s}^{-} \\ X_{s}^{-} \\ X_{t}^{-} \end{cases}$
+	Q _m 0 0 0	0 Q _b 0 0	0 0 <i>C_b</i> 0	0 0 0 <i>C_t</i>	$\begin{bmatrix} \theta_m \\ \theta_s \\ X_s \\ X_t \end{bmatrix}$

$$+ \begin{bmatrix} K_{t} & -K_{t} & 0 & 0 \\ -K_{t} & K_{t} + K_{n}R^{2} & K_{n}R & -K_{n}R \\ 0 & K_{n}R & K_{a} + K_{n} & -K_{n} \\ 0 & -K_{n}R & -K_{n} & K_{n} \end{bmatrix} \begin{bmatrix} \theta_{m} \\ \theta_{s} \\ X_{s} \\ X_{t} \end{bmatrix}$$

$$= \begin{bmatrix} T \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

This mathematical model is used to make simulation of ball screw feed drive system and study the effect of various parameters in the dynamic behavior of the system.

B. Simulation of Feed Drive System -

The four states in the above matrix equation are θ_m refers to rotation displacement of motor, θ_s refers to rotation displacement of the ball screw shaft, X_s refers to axial displacement of the ball screw shaft and X_t refers to axial displacement of the working table. The values and states of this model are defined in table (1).

Table -1. The values of experimental set up used in numerical simulation

Parameter of the component	Value	
$J_m(kg.m^2)$	4.8 ×10 ⁻⁵	
J _s (kg.m ²)	0.495×10 ⁻⁴	
M _s (kg)	1.8	
M _t (kg)	0.373	
Qm (N.s/m)	0	
Q _b (N.s/m)	0	
C _b (N.s/m)	0	
Parameter of the component	Value	
C _t (N.s/m)	0	
K _n (N/m)	0.4689× 10 ⁷	



K _t (N.m/rad)	496.7	
K _a (N/m)	0.3619× 10 ⁸	
R	0.0025	
T(N.m)	1.3	

IV. RESULTS

The equation of motion of the lumped parameters of ball screw feed drive system can be used to represent the transient response of the system. The motor torque represent the force applied to the system. The natural frequencies of the model are 6.1035×10^{-5} rad/sec, 3.1636×10^{3} rad/sec, 4.5115×10^{3} rad/sec and 5.0886×10^{3} rad/sec. the mode shape vectors V1, V2, V3, and V4 of the model as shown in table (2).

Table -2. Shows the various mode shape for " θ_m , θ_s , X_s and X"

At							
The first	The first The second		The fourth				
mode mode		mode	mode				
V1=0.7071	V2=-0.9980	V3=-0.7189	V4=-0.5540				
0.7071	-0.0327	0.6951	0.8323				
0.0000	0.0109	-0.0018	0.0145				
0.0018	0.0531	0.0001	-0.0157				

The bode diagram which involves the graphical representation of the frequency responses of a single axis ball screw feed drive system is shown in Fig. (3).



Fig. (3): Bode diagram of a ball screw feed drive system

Bode diagram of the dynamic system based on different values of table mass is shown in Fig. (4). The three different values of table masses are 110%, 100% and 90% of the rated table mass which its value equal to 0.373 kg as shown in table (1). So the three different masses are 0.4103 kg, 0.373 kg and 0.3357 kg respectively.



Fig. (4): Bode diagram of table mass



Fig. (5): The enlargement of the second mode of the Bode diagram shown in Fig. (4)





Fig. (6): The enlargement of the fourth mode of the Bode diagram shown in Fig. (4)

The bode diagram of the dynamic system based on different values of stiffness of the nut is shown in Fig. (7). The three different values of stiffness of the ball nut are 110%, 100% and 90% of the value of the rated stiffness of the nut which its value equal to 0.4689×10^7 N/m as shown in table (1). So the three different stiffness of nut are 0.51579×10^7 N/m, 0.4689×10^7 N/m and 0.42201×10^7 N/m respectively.



Fig. (7): Bode diagram of stiffness of the nut



Fig. (8): The enlargement of the second mode of the Bode diagram in Fig. (7)



Fig. (9): The enlargement of the fourth mode of the Bode diagram in Fig. (7)

The bode diagram of the dynamic system based on different values of axial stiffness of the ball screw shaft is shown in Fig. (10). The three different values of axial stiffness of the ball screw shaft are 110%, 100% and 90% of the value of the rated axial stiffness of the ball screw shaft which its value equal to 0.3619×10^8 N/m as shown in table (1). So the three different axial stiffness of the ball screw shaft are 0.39809×10^8 N/m, 0.3619×10^8 N/m and 0.32571×10^8 N/m respectively.





Fig. (10): Bode diagram of axial stiffness of the ball screw shaft



Fig. (11): The enlargement of the second mode of the Bode diagram in Fig. (10)



Fig. (12): The enlargement of the fourth mode of the Bode diagram in Fig. (10)

The bode diagram of the dynamic system based on different values of torsional stiffness of the ball screw is shown in Fig. (13). The three different values of torsional stiffness of the ball screw are 110%, 100% and 90% of the value of the rated torsional stiffness of the ball screw which its value equal to 496.7 N.m/rad as shown in table (1). So the three different torsional stiffness of the ball screw are 546.37 N.m/rad, 496.7 N.m/rad and 447.03 N.m/rad respectively.



Fig. (13): Bode diagram of torsional stiffness of the ball screw





Fig. (14): The enlargement of the third mode of the Bode diagram in Fig. (13)

V. DISCUSSION OF RESULTS

Enlargement of the second and fourth modes of the bode diagram are shown in Figures (5&6). The frequency change in the first and third modes is very small. In second mode the frequency changes from 3.1636×10^3 Hz to 3.04×10^3 Hz in case of increase table mass by 10%, and to 3.3×10^3 Hz in case of decreasing table mass by 10%. In fourth mode the frequency changes from 5.0886×10^3 Hz to 5.05×10^3 Hz in case of increase table mass by 10%, and to 5.14×10^3 Hz in case of decrease table mass by 10%. It is obvious that the second and fourth modes will be affected more than other modes when the mass table is varying.

As expected when the mass of table increase the vibration fundamental frequency decreased because the frequency is inversely proportional to the mass (frequency $\propto 1/\text{mass}$) so when the mass of table increased by 10% we noticed that the frequency decreased. And vice versa when mass of table decreased by 10% the frequency increased.

Enlargement of the second and fourth modes of the bode diagram are shown in Figures (8&9). In second mode the frequency changes from 3.1636×10^3 Hz to 3.26×10^3 Hz in case of increase stiffness of the ball nut by 10%, and to 3.05×10^3 Hz in case of decrease stiffness of the ball nut by 10%. In fourth mode the frequency changes from 5.0886×10^3 Hz to 5.18×10^3 Hz in case of increase stiffness of the ball nut by 10%, and to 5×10^3 Hz in case of decrease stiffness of the ball nut by 10%, and to 5×10^3 Hz in case of decrease stiffness of the ball nut by 10%.

Enlargement of the second and fourth modes of the bode diagram are shown in Figures (11&12). In second mode the frequency changes from 3.1636×10^3 Hz to 3.21×10^3 Hz in case of increase axial stiffness of the ball screw shaft by 10%, and to 3.1×10^3 Hz in case of decrease axial stiffness of the ball screw shaft by 10%. In fourth mode the frequency changes from 5.0886×10^3 Hz to 5.24×10^3 Hz in case of increase axial stiffness of the ball screw shaft by 10%, and to 4.95×10^3 Hz

in case of decrease axial stiffness of the ball screw shaft by 10%.

Enlargement of third mode of the bode diagram shown in Fig. (14). The frequency change in the first and second modes is very small. In third mode the frequency changes from 4.5115×10^3 Hz to 4.7×10^3 Hz in case of increase torsional stiffness of the ball screw by 10%, and to 4.3×10^3 Hz in case of decrease torsional stiffness of the ball screw by 10%.

The frequency of the system increases with increasing the stiffness because the relation between them is $\omega 2$ =k/m where ω the natural frequency, k stiffness, m mass. So the frequency is directly proportional to the stiffness (frequency \propto stiffness). As shown in results, with increasing the stiffness of nut or torsional stiffness of ball screw or axial stiffness of ball screw the frequency of the system increase.

The frequency of the system increases with increasing the stiffness of nut or the torsional stiffness of ball screw or the axial stiffness of ball screw as shown in the previous results because the relation between them is $\omega^2 = k/m$ where ω the natural frequency, k stiffness, m mass.

VI. CONCLUSION

The change in displacements arrangement of the system cause change in both phase angles and chart trend while the frequencies still the same.

The numerical simulation of a lumped parameter model by using different values of table mass, stiffness of the ball nut, axial stiffness of the ball screw shaft and torsional stiffness of the ball screw describe changes in dynamic behavior of the system. Effects of each parameter in this model can be diagnosed by determining the change in value of frequency peaks.

The inertia moment of both the motor and ball screw system did not have any significant effect in the system performance.

When changing by increasing or decreasing the values of the investigated parameters, the rotation displacement of the ball screw and the axial displacement of the working table have the biggest effect more than other states.

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